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N, n	Particle number, particle number density	∇^2	Laplace operator $= \partial^2/\partial x^2 + \partial^2/\partial y^2 + \partial^2/\partial z^2$
N	Normalisation factor	ΔE	Energy uncertainty
n	Principal quantum number or number of photons or an integer	Δk	Wavenumber uncertainty
P	Spectral radiation flux density (5.2) or probability	Δp	Momentum uncertainty
P_l^0	Legendre polynomial	Δt	Time uncertainty (= finite measurement time)
P_l^m	($m \neq 0$) Associated Legendre function	ΔV	Finite volume element
$p, \bar{p}$	Momentum, expectation value of momentum	$\Delta \omega$	Uncertainty in the angular frequency
Q	Nuclear quadrupole moment (20.20)	Δx	Position uncertainty
Q, q	Charge	$\delta(x)$	Dirac delta function (see mathematics appendix)
$R(r)$	Radial part of the hydrogen wavefunction	$\delta_{\mu, \nu}$	Kronecker delta symbol: $\delta_{\mu, \nu} = 1$ for $\mu = \nu$, $\delta_{\mu, \nu} = 0$ for $\mu \neq \nu$
r	Position coordinate (three-dimensional vector)	ε	Dimensionless energy (9.83)
r	Distance	$\varepsilon^{(n)}$	Energy contributions to perturbation theory
S	Resultant spin (17.4)	ε_0	Permittivity constant of vacuum
S	Symbol for orbital angular momentum $L = 0$	θ	Angle coordinate (10.2)
s, s	Electron spin and corresponding quantum number (12.15)	κ	Defined in (10.54)
$\hat{s}$	Spin operator $= (\hat{s}_x, \hat{s}_y, \hat{s}_z)$	λ	Wavelength (exception: expansion parameter in [15.2.1, 2])
T	Absolute temperature	μ, μ	Magnetic moment (12.1)
T_1	Longitudinal relaxation time	μ	Reduced mass (8.15)
T_2	Transverse relaxation time	μ_B	Bohr magneton (12.8)
t	Time	μ_N	Nuclear magneton (20.3)
u	Spectral energy density (5.2), atomic mass unit [2.2]	ν	Frequency [8.1]
V	Volume, potential, electric voltage	$\bar{\nu}$	Wavenumber [8.1]
$\bar{V}$	Expectation value of the potential energy	ξ	Dimensionless coordinate (9.83)
v	Velocity, particle velocity	ϱ	Charge density, density of states, mass density; or dimensionless distance
x	Particle coordinate (one-dimensional)	σ	Scattering coefficient, interaction cross section (2.16)
$\bar{x}$	Expectation value of position	τ	Torque (12.2)
$Y_{l,m}(\theta, \phi)$	Spherical harmonic functions (10.10, 48–50)	Φ	Phase
Z	Nuclear charge	ϕ	Phase angle, angle coordinate
α	Fine structure constant [8.10] or absorption coefficient (2.22)	$\phi(x)$	Wavefunction of a particle
β	Constant	$\phi_{\uparrow}, \phi_{\downarrow}, \phi$	Spin wavefunctions
Γ	Decay constant	ψ	Wavefunction
γ	Decay constant or linewidth gyromagnetic ratio (12.12)	Ψ	Wavefunction of several electrons
		$\hat{\Omega}$	Generalised quantum mechanical operator
		Ω	Frequency [14.4, 14.5, 15.3]
		ω	Angular frequency $2\pi\nu$, or eigenvalue [9.3.6]
		$\triangleq$	means “corresponds to”