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Nonequilibrium Phase Transitions in Semiconductors

Self-Organization Induced by
Generation and Recombination Processes

With 165 Figures

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