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Data Analysis Using the Method of Least Squares

Extracting the Most Information from Experiments

With 58 Figures and 68 Tables



Springer

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