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## **Spectral Theory of Linear Operators**

and Spectral Systems in Banach Algebras

Second edition

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