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Binding and Scattering in Two-Dimensional Systems

Applications to Quantum Wires,
Waveguides and Photonic Crystals



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