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Fundamentals of Quantum Information

Quantum Computation, Communication,
Decoherence and All That



Springer

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