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Statistical Analysis of Extreme Values

with Applications to Insurance, Finance,
Hydrology and Other Fields

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