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Vision with Direction

A Systematic Introduction
to Image Processing and Computer Vision

With 146 Figures, including 130 in Color

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