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Fast Simulation of Electro-Thermal MEMS

Efficient Dynamic Compact Models

With 108 Figures, 8 in Color and 9 Tables

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