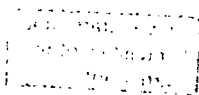


Michel Talagrand

The Generic Chaining

Upper and Lower Bounds
of Stochastic Processes



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