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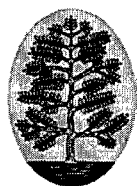
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The Global Theory of Minimal Surfaces in Flat Spaces

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