

Conformal Algebra in Space-Time and Operator Product Expansion*

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Contents

1. Introduction	2
2. Introduction to the Conformal Group in Space-Time	8
2.1. The Conformal Group	8
2.2. Mass Spectrum	10
2.3. Representations	10
2.4. Conformal Currents	12
3. Broken Conformal Symmetry	17
3.1. Broken Conformal Symmetry and the Energy Momentum Tensor	17
3.2. Equal Time Commutators among the Conformal Charges	19
4. Restrictions from Conformal Covariance on Equal-Time Commutators	24
4.1. Outline of the Problem	24
4.2. Summary of General Properties of Equal Time Commutators	25
4.3. Restrictions from Lorentz Covariance on Equal-Time Commutators	27
4.4. Restrictions on Equal-Time Commutators Ensuing from Conformal Symmetry	28
5. Manifestly Conformal Covariant Structure of Space-Time	29
5.1. Spinor Operators	29
5.2. Irreducible Representations in Space-Time	31
5.3. Structure of Representations and Connections with $O(4,2)$ Covariant Tensors	31
5.4. "Canonical Dimensions"	33
6. Conformal Invariant Vacuum Expectation Values	34
6.1. Two-Point Functions	34
6.2. Three Point-Functions	37
7. Operator Products and Conformal Invariance on the Light-Cone	38
7.1. Operator Product Expansions on the Light-Cone	38
7.2. Properties of the Light-Cone Expansion	42
7.3. Causality on the Light-Cone	43
8. Consequences of Exact Conformal Symmetry on Operator Product Expansions	45
8.1. Operator Expansions on Space-Time	45
8.2. Properties of the Strictly Conformal Covariant Operator Expansion	48
8.3. Connection with the Three-Point Function	49
9. Conclusions and Outlook	52
Appendices: A, B, C, D, E	53
References	61
Classified Index of Authors and Titles. Volumes 36–68	65

* Dedicated to Prof. G. Höhler on his 50th birthday.