## **Contents**

|   |      | •  |     |                                   |       |      |   |   |
|---|------|----|-----|-----------------------------------|-------|------|---|---|
|   | 101  | Λt | 201 | \ra\                              | iatio | anc. |   | X |
| L | .13t | vı | avı | $\mathcal{I} \subset \mathcal{I}$ | ıatı  | UIIO | _ | ^ |

List of notations --- xiii

| 1 | Introduction — | 1 |
|---|----------------|---|
|---|----------------|---|

| 2       | Fiber ring interferometry — 8   |
|---------|---|
| 2.1     | Sagnac effect. Correct and incorrect explanations — 8                     |
| 2.1.1   | Correct explanations of the Sagnac effect — 8                             |
| 2.1.1.1 | Sagnac effect in special relativity — 8                                   |
| 2.1.1.2 | Sagnac effect in general relativity — 9                                   |
| 2.1.1.3 | Methods for calculating the Sagnac phase shift in anisotropic             |
|         | media — 9   |
| 2.1.2   | Conditionally correct explanations of the Sagnac effect — 10              |
| 2.1.2.1 | Sagnac effect due to the difference between the non-relativistic          |
|         | gravitational scalar potentials of centrifugal forces in reference frames |
|         | moving with counterpropagating waves — 10                                 |
| 2.1.2.2 | Sagnac effect due to the sign difference between the non-relativistic     |
|         | gravitational scalar potentials of Coriolis forces in reference frames    |
|         | moving with counterpropagating waves — 10                                 |
| 2.1.2.3 | Quantum mechanical Sagnac effect due to the influence of the Coriolis     |
|         | force vector potential on the wave function phases of                     |
|         | counterpropagating waves in rotating reference frames — 11                |
| 2.1.3   | Attempts to explain the Sagnac effect by analogy with other               |
|         | effects — 11  |
| 2.1.3.1 | Analogy between the Sagnac and Aharonov–Bohm effects — 11                 |
| 2.1.3.2 | Sagnac effect as a manifestation of the Berry phase —— 12                 |
| 2.1.4   | Incorrect explanations of the Sagnac effect —— 12                         |
| 2.1.4.1 | Sagnac effect in the theory of a quiescent luminiferous ether — 12        |
| 2.1.4.2 | Sagnac effect from the viewpoint of classical kinematics — 13             |
| 2.1.4.3 | Sagnac effect as a manifestation of the classical Doppler effect from     |
|         | a moving splitter —— 14   |
| 2.1.4.4 | Sagnac effect as a manifestation of the Fresnel–Fizeau dragging           |
|         | effect — 15   |
| 2.1.4.5 | Sagnac effect and Coriolis forces — 15                                    |
| 2.1.4.6 | Sagnac effect as a consequence of the difference between the orbital      |
|         | angular momenta of photons in counterpropagating waves —— 16              |
| 2.1.4.7 | Sagnac effect as a manifestation of the inertial properties of            |
|         | an electromagnetic field —— 16  |

| 2.1.4.8 | Sagnac effect in incorrect theories of gravitation —— 16             |
|---------|--|
| 2.1.4.9 | Other incorrect explanations of the Sagnac effect — 17               |
| 2.2     | Physical problems of the fiber ring interferometry — 17              |
| 2.2.1   | Milestones of the creation and development of optical ring           |
|         | interferometry and gyroscopy based on the Sagnac effect — 17         |
| 2.2.2   | Sources for additional nonreciprocity of fiber ring                  |
|         | interferometers — 20   |
| 2.2.2.1 | General characterization of sources for additional nonreciprocity of |
|         | fiber ring interferometers — 20                                      |
| 2.2.2.2 | Nonreciprocity as a consequence of the light source coherence — 21   |
| 2.2.2.3 | Polarization nonreciprocity: causes and solutions — 21               |
| 2.2.2.4 | Nonreciprocity caused by local variations in the gyro fiber-loop     |
|         | parameters due to variable acoustic, mechanical, and temperature     |
|         | actions — 23   |
| 2.2.2.5 | Nonreciprocity due to the Faraday effect in external magnetic        |
|         | field — 23   |
| 2.2.2.6 | Nonreciprocal effects caused by nonlinear interaction between        |
|         | counterpropagating waves (optical Kerr effect) — 23                  |
| 2.2.2.7 | Nonreciprocity caused by relativistic effects in fiber ring          |
|         | interferometers — 24   |
| 2.2.3   | Fluctuations and ultimate sensitivity of fiber ring                  |
|         | interferometers — 24   |
| 2.2.4   | Methods for achieving the maximum sensitivity to rotation and        |
|         | processing the output signal — 25                                    |
| 2.2.5   | Applications of fiber optic gyroscopes and fiber ring                |
| -       | interferometers — 26   |
| 2.3     | Physical mechanisms of random coupling between polarization          |
|         | modes — 28   |
| 2.3.1   | Milestones of the development of the theory of polarization mode     |
|         | linking in single-mode optical fibers — 28                           |
| 2.3.2   | Phenomenological models of polarization mode coupling — 30           |
| 2.3.3   | Physical models of polarization mode coupling — 31                   |
| 2.3.4   | Inhomogeneities arising as a fiber is drawn —— 32                    |
| 2.3.4.1 | Torsional vibration —— 32  |
| 2.3.4.2 | Longitudinal vibration — 33  |
| 2.3.4.3 | Transverse vibration — 33  |
| 2.3.4.4 | Transverse stresses — 34   |
| 2.3.5   | Inhomogeneities arising in applying protective coatings — 34         |
| 2.3.6   | Inhomogeneities arising in the course of winding — 34                |
| 2.3.7   | Rayleigh scattering: the fundamental cause of polarization mode      |
|         | coupling — 35  |
| 2.4     | Application of the Poincaré sphere method — 35                       |
| 2.5     | Thomas precession. Interpretation and observation issues — 36        |
| 2.4     | coupling — 35 Application of the Poincaré sphere method — 35         |

| 3     | Development of the theory of interaction between polarization modes —— 38   |
|-------|---|
| 3.1   | Phenomenological estimates of the random coupling — 38  |
| 3.1.1 | Small perturbation method — 38  |
| 3.1.2 | Expanding the scope of the small perturbation method by partitioning the fiber into segments whose length is equal to the depolarization length —— 40 |
| 3.2   | A physical model of the polarization mode coupling — 41   |
| 3.2.1 | A model of random inhomogeneities in SMFs with random twists of the anisotropy axes —— 41   |
| 3.2.2 | Connection between the polarization holding parameter and statistics of random inhomogeneities —— 42  |
| 3.2.3 | Polarization holding parameter in the case of random and regular twisting —— 45   |
| 3.2.4 | Statistical properties of the polarization modes for fibers with random inhomogeneities —— 47   |
| 3.3   | Evolution of the degree of polarization of nonmonochromatic light — 55  |
| 3.3.1 | Small perturbation method — 55  |
| 3.3.2 | A method for modeling random twists — 57  |
| 3.3.3 | A mathematical method for modeling random twists in the presence of a regular twist —— 63   |
| 3.3.4 | Analytical calculation of the limiting degree of polarization of nonmonochromatic light —— 68   |
| 3.3.5 | Increasing of the correlation length of nonmonochromatic light traveling through a single-mode fiber with random inhomogeneities — 69                 |
| 3.4   | Anholonomy of the evolution of light polarization — 72  |
| 4     | Experimental study of random coupling between polarization modes — 76   |
| 4.1   | A rapid method for measuring the output polarization state — 76   |
| 4.2   | Method for measuring the polarization beat length and ellipticity —— 79   |
| 4.3   | Experimental comparison of the accuracy of different methods — 86   |
| 4.4   | Influence of winding of single-mode fibers on the amount of the polarization holding parameter — 89   |
| 4.5   | Experimental study of the polarization degree evolution of light — 92   |
| 4.6   | Method of fabricating ribbon single-mode fibers — 93  |
| 4.7   | Method for removing the effect of photodetector dichroism — 95  |
| 5     | Fiber ring interferometers of minimum configuration — 98  |
| 5.1   | Polarization nonreciprocity of fiber ring interferometers — 98  |
| 5.2   | Fiber ring interferometers with a single-mode fiber circuit — 107   |

| 5.3     | Zero shift, deviation, and drift of fiber ring interferometers — 110     |
|---------|--|
| 5.3.1   | Applicability conditions for the ergodic hypothesis — 110                |
| 5.3.2   | Influence of the amount of random twist of the fiber — 131               |
| 5.3.3   | Influence of the location of the random inhomogeneity —— 131             |
| 5.3.4   | Influence of the mutual coherence of nonmonochromatic light in           |
|         | the main and orthogonal polarization modes at the point of               |
|         | inhomogeneity —— 132   |
| 5.3.5   | Approximate calculation of the temperature zero drift — 132              |
| 5.3.6   | Calculation of the zero shift deviation of the FRI by the small          |
|         | perturbation method —— 136   |
| 5.3.7   | Calculation of the zero shift deviation with the extended small          |
|         | perturbation method — 139  |
| 5.3.8   | Calculation of the zero shift deviation by the method of mathematical    |
|         | modeling of random inhomogeneities — 139                                 |
| 5.3.8.1 | Zero shift deviation of an FRI with a high-birefringence fiber — 140     |
| 5.3.8.2 | Zero shift deviation of an FRI with a low-birefringence fiber — 142      |
| 5.3.9   | Calculation of the zero shift deviation of FRIs 144                      |
| 5.4     | Domains of application of the different methods for calculating          |
|         | PN 146   |
|         |  |
| 6       | Fiber ring interferometers of nonstandard configuration — 148            |
| 6.1     | New type of nonmonochromatic light depolarizer for FRIs — 148            |
| 6.2     | Zero drift and output signal fading in an FRI with a polarizer — 156     |
| 6.2.1   | Small perturbation method. The quasi-axis model — 156                    |
| 6.2.2   | Extended small perturbation method — 157                                 |
| 6.2.3   | Method of mathematical modeling of random inhomogeneities in             |
|         | fibers — 158   |
| 6.3     | Fiber ring interferometers without a polarizer — 163                     |
| 6.3.1   | FRIs with circularly polarized input light — 164                         |
| 6.3.2   | Modulation method for removing the zero shift in a fiber ring            |
|         | interferometer without a polarizer — 167                                 |
| 6.3.3   | Fiber ring interferometer with a depolarizer of nonmonochromatic         |
|         | light — 169  |
| 6.3.4   | Fiber ring interferometer with a circuit made from a uniformly twisted   |
|         | fiber — 170  |
| 6.3.5   | Zero shift deviation in FRIs without a polarizer and with a circuit made |
|         | from a high-birefringence fiber in a limited temperature range — 171     |
| 7       | Geometric phases in optics. The Poincaré sphere method — 172             |
| 7.1     | Application of the Poincaré sphere method — 172                          |
| 7.1.1   | Analysis of the properties of the Pancharatnam phases. The Poincaré      |
| ,,,,,   | sphere —— 172  |
|         |  |

| 7.1 | .1.1 | Type I Pancharatnam phase —— 172   |
|-----|------|--|
| 7.1 | .1.2 | Type II Pancharatnam phase —— 173  |
| 7.1 | .2   | Birefringence in SMFs due to mechanical deformations — 175   |
| 7.1 | .2.1 | Kinematic phase in SMFs — 175  |
| 7.1 | .2.2 | Bending induced linear birefringence of SMFs — 176   |
| 7.1 | .2.3 | Twisting-induced circular birefringence of SMFs. The spiral polarization                                     |
|     |      | modes 176  |
| 7.1 | .3   | Rytov effect and the Rytov-Vladimirskii phase in SMFs and FRIs in  |
|     |      | the case of noncoplanar winding — 177  |
| 7.1 | .3.1 | Rytov effect in the FRI circuit fiber —— 177   |
| 7.1 | .3.2 | Rytov-Vladimirskii phase and PP2 in SMFs with noncoplanar  |
|     |      | winding — 179  |
| 7.1 | .3.3 | Rytov phase detection in FRIs —— <b>180</b>  |
| 7.2 |      | Polarization nonreciprocity in FRIs. Nonreciprocal geometric   |
|     |      | phase —— <b>182</b>  |
| 7.3 |      | Determination of a polarization state ensuring the absence of  |
|     |      | NPDCM — 189  |
| 7.4 |      | Criticism of unsubstantiated hypotheses relating to geometric  |
|     |      | phases — 191   |
| 7.5 |      | Opto-mechanical analogies relating to light propagation in   |
|     |      | SMFs — 195   |
| 7.5 | .1   | The analogy between the Rytov effect polarization optics and Ishlinskii                                      |
|     |      | effect in classical mechanics — 195  |
| 7.5 | .2   | An opto-mechanical analogy of an SMF with twisting of the linear   |
|     |      | birefringence axes — 198   |
| 8   | Tin  | no dependent nonlinear and magnetic effects 201  |
| 8.1 |      | ne-dependent, nonlinear, and magnetic effects — 201 Influence of the second harmonic of the phase modulation |
| 0.1 |      | frequency — 201  |
| 8.1 | 1    | In-phase and quadrature components of the parasitic phase  |
| 0.1 |      | modulation — 201   |
| 8.1 | .2   | Numerical estimates of the incidental phase modulation — 203   |
| 8.1 |      | Optimal harmonic of the phase modulation frequency — 206   |
| 8.2 |      | Experimental investigation of the piezo transducer's   |
| 0.2 | •    | nonlinearity — 207   |
| 8.3 | ;    | Methods for removing the influence of the nonlinear Kerr effect — 209  |
| 8.4 |      | Influence of random inhomogeneities on the Faraday zero shift  |
|     |      | deviation — 215  |
| 9   | Re   | lativistic effects in optical and non-optical ring interferometers — 220                                     |
| 9.1 |      | Sagnac effect for waves of any nature in special relativity — 220  |
| 9.1 | .1   | Sagnac effect in the laboratory frame of reference — 220   |
|     |      |  |

| 9.1.2   | Sagnac effect in a rotating frame of reference. Zeno's relativistic      |
|---------|--|
|         | paradox — 223  |
| 9.2     | Non-optical Sagnac sensors of angular velocity — 226                     |
| 9.2.1   | A ring interferometer based on slow acoustic or magnetic                 |
|         | waves —— 226   |
| 9.2.1.1 | Advantages of using slow waves in ring interferometers — 226             |
| 9.2.1.2 | Choosing an optimal frequency of the slow waves in ring                  |
|         | interferometers — 227  |
| 9.2.1.3 | A method for detecting the phase difference between                      |
|         | counterpropagating waves in slow-wave ring interferometers — 229         |
| 9.2.2   | A ring interferometer based on de Broglie waves of pions — 232           |
| 9.3     | Influence of Thomas precession on the zero shift — 236                   |
| 9.3.1   | Thomas precession as a corollary of Ishlinskii's solid angle theorem     |
|         | applied to the angle of relativistic aberration — 236                    |
| 9.3.1.1 | Thomas precession —— 236   |
| 9.3.1.2 | Ishlinskii's theorem as a classical analogue of Thomas                   |
|         | precession — 237   |
| 9.3.1.3 | Observed rotation of an object rapidly moving in a circular path and     |
|         | Thomas precession —— 238   |
| 9.3.1.4 | Physical meanings of the Thomas precession and Ishlinskii                |
|         | angle — 241  |
| 9.3.2   | Influence of Thomas precession on the zero shift of ring interferometers |
|         | based on de Broglie waves of matter particles with spin — 241            |
| 9.4     | Potential usage of FRIs for detecting fundamental effects — 243          |
| 9.4.1   | Verification of the basic postulates of special and general relativity   |
|         | using FRIs — 243   |
| 9.4.2   | Analysis of the possibility of detecting nonreciprocal effects with      |
|         | FRIs — 246   |
|         |  |

10 Conclusion — 250

Index — 299