

Gerhard Winkler

Image Analysis, Random Fields and Dynamic Monte Carlo Methods

A Mathematical Introduction

With 59 Figures



Springer

Table of Contents

Introduction	1
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Part I. Bayesian Image Analysis: Introduction

1. The Bayesian Paradigm.....	13
1.1 The Space of Images	13
1.2 The Space of Observations	15
1.3 Prior and Posterior Distribution	16
1.4 Bayesian Decision Rules	19
2. Cleaning Dirty Pictures	23
2.1 Distortion of Images	23
2.1.1 Physical Digital Imaging Systems.....	23
2.1.2 Posterior Distributions	26
2.2 Smoothing.....	29
2.3 Piecewise Smoothing	35
2.4 Boundary Extraction	43
3. Random Fields	47
3.1 Markov Random Fields	47
3.2 Gibbs Fields and Potentials	51
3.3 More on Potentials	57

Part II. The Gibbs Sampler and Simulated Annealing

4. Markov Chains: Limit Theorems.....	65
4.1 Preliminaries.....	65
4.2 The Contraction Coefficient.....	69
4.3 Homogeneous Markov Chains	73
4.4 Inhomogeneous Markov Chains.....	76

5. Sampling and Annealing	81
5.1 Sampling	81
5.2 Simulated Annealing	88
5.3 Discussion	94
6. Cooling Schedules	99
6.1 The ICM Algorithm	99
6.2 Exact MAPE Versus Fast Cooling	102
6.3 Finite Time Annealing	111
7. Sampling and Annealing Revisited	113
7.1 A Law of Large Numbers for Inhomogeneous Markov Chains ..	113
7.1.1 The Law of Large Numbers	113
7.1.2 A Counterexample	118
7.2 A General Theorem	121
7.3 Sampling and Annealing under Constraints	125
7.3.1 Simulated Annealing	126
7.3.2 Simulated Annealing under Constraints	127
7.3.3 Sampling with and without Constraints	129

Part III. More on Sampling and Annealing

8. Metropolis Algorithms	133
8.1 The Metropolis Sampler	133
8.2 Convergence Theorems	134
8.3 Best Constants	139
8.4 About Visiting Schemes	141
8.4.1 Systematic Sweep Strategies	141
8.4.2 The Influence of Proposal Matrices	143
8.5 The Metropolis Algorithm in Combinatorial Optimization ...	148
8.6 Generalizations and Modifications	151
8.6.1 Metropolis-Hastings Algorithms	151
8.6.2 Threshold Random Search	153
9. Alternative Approaches	155
9.1 Second Largest Eigenvalues	155
9.1.1 Convergence Reproved	155
9.1.2 Sampling and Second Largest Eigenvalues	159
9.1.3 Continuous Time and Space	163
10. Parallel Algorithms	167
10.1 Partially Parallel Algorithms	168
10.1.1 Synchronous Updating on Independent Sets	168
10.1.2 The Swendsen-Wang Algorithm	171

10.2 Synchronous Algorithms	173
10.2.1 Introduction	173
10.2.2 Invariant Distributions and Convergence	174
10.2.3 Support of the Limit Distribution	178
10.3 Synchronous Algorithms and Reversibility	182
10.3.1 Preliminaries	183
10.3.2 Invariance and Reversibility	185
10.3.3 Final Remarks	189

Part IV. Texture Analysis

11. Partitioning	195
11.1 Introduction	195
11.2 How to Tell Textures Apart	195
11.3 Features	196
11.4 Bayesian Texture Segmentation	198
11.4.1 The Features	198
11.4.2 The Kolmogorov-Smirnov Distance	199
11.4.3 A Partition Model	199
11.4.4 Optimization	201
11.4.5 A Boundary Model	203
11.5 Julesz's Conjecture	205
11.5.1 Introduction	205
11.5.2 Point Processes	205
12. Texture Models and Classification	209
12.1 Introduction	209
12.2 Texture Models	210
12.2.1 The Φ -Model	210
12.2.2 The Autobinomial Model	211
12.2.3 Automodels	213
12.3 Texture Synthesis	214
12.4 Texture Classification	216
12.4.1 General Remarks	216
12.4.2 Contextual Classification	218
12.4.3 MPM Methods	219

Part V. Parameter Estimation

13. Maximum Likelihood Estimators	225
13.1 Introduction	225
13.2 The Likelihood Function	225

13.3 Objective Functions	230
13.4 Asymptotic Consistency	233
14. Spatial ML Estimation	237
14.1 Introduction	237
14.2 Increasing Observation Windows	237
14.3 The Pseudolikelihood Method	239
14.4 The Maximum Likelihood Method	246
14.5 Computation of ML Estimators	247
14.6 Partially Observed Data	253

Part VI. Supplement

15. A Glance at Neural Networks	257
15.1 Introduction	257
15.2 Boltzmann Machines	257
15.3 A Learning Rule	262
16. Mixed Applications	269
16.1 Motion	269
16.2 Tomographic Image Reconstruction	274
16.3 Biological Shape	276

Part VII. Appendix

A. Simulation of Random Variables	283
A.1 Pseudo-random Numbers	283
A.2 Discrete Random Variables	286
A.3 Local Gibbs Samplers	289
A.4 Further Distributions	290
A.4.1 Binomial Variables	290
A.4.2 Poisson Variables	292
A.4.3 Gaussian Variables	293
A.4.4 The Rejection Method	296
A.4.5 The Polar Method	297
B. The Perron-Frobenius Theorem	299
C. Concave Functions	301
D. A Global Convergence Theorem for Descent Algorithms ..	305
References	307
Index	321