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Electron-Beam Interactions with Solids

Application of the Monte Carlo Method
to Electron Scattering Problems

With 27 Figures



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