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# Syntax-Directed Semantics

Formal Models  
Based on Tree Transducers

With 74 Figures



Springer

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