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# Theoretical Physics

## A Classical Approach

Translated by H. Pollack With 141 Figures and 39 Problems

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