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Encounter with Chaos

Self-Organized Hierarchical Complexity
in Semiconductor Experiments

With 182 Figures

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