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| <b>E</b> | <b>Glossary</b>                                      | <b>737</b> |
|          | <b>Index</b>                                         | <b>745</b> |