

PART I

Meinhard E. Mayer, <u>Introduction to the Fiber-Bundle Approach</u> <u>to Gauge Theories</u>	1
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PART II

Wolfgang Drechsler, <u>Gauge Theory of Strong and Electromagnetic</u> <u>Interactions Formulated on a Fiber Bundle</u> <u>of the Cartan Type</u>	145
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