

# OPTIONS, FUTURES, AND OTHER DERIVATIVES

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# OPTIONS, FUTURES, AND OTHER DERIVATIVES

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# ELEVENTH EDITION GLOBAL EDITION



# Options, Futures, and Other Derivatives, Global Edition

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