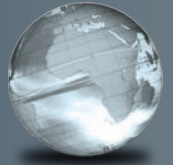


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Econometric Analysis

EIGHTH EDITION

William H. Greene



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ECONOMETRIC ANALYSIS



William H. Greene

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