
THE CLASSIC WORK
EXTENDED AND REFINED

The Art of Computer Programming

VOLUME 4B

Combinatorial Algorithms

Part 2

DONALD E. KNUTH

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Art of Computer Programming, Volume 4B, The: Combinatorial Algorithms

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