
THE CLASSIC WORK
NEWLY UPDATED AND REVISED

The Art of Computer Programming

VOLUME 1

Fundamental Algorithms
Third Edition

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Art of Computer Programming, The: Volume 1: Fundamental Algorithms

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